Machine learning and statistical analyses for extracting and characterizing “fingerprints” of antibody aggregation at container interfaces from flow microscopy images

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Abstract
Therapeutic proteins are exposed to numerous stresses during their manufacture, shipping, storage and administration to patients, causing them to aggregate and form particles through a variety of different mechanisms. These varied mechanisms generate particle populations with characteristic morphologies, creating “fingerprints” that are reflected in images recorded using flow imaging microscopy. Particle population fingerprints in test samples can be extracted and compared against those of particles produced under baseline conditions using an algorithm that combines machine learning tools such as convolutional neural networks with statistical tools such as nonparametric density estimation and Rosenblatt transform-based goodness-of-fit hypothesis testing. This analysis provides a quantitative method with user-specified type 1 error rates to determine whether the mechanisms that produce particles in test samples differ from particle formation mechanisms operative under baseline conditions. As a demonstration, this algorithm was used to compare particles within intravenous immunoglobulin formulations that were exposed to freeze-thawing and shaking stresses within a variety of different containers. This analysis revealed that seemingly subtle differences in containers (e.g., glass vials from different manufacturers) generated distinguishable particle populations after the stresses were applied. This algorithm can be used to assess the impact of process and formulation changes on aggregation-related product instabilities.

KEYWORDS
image analysis, machine learning, protein aggregation, protein formulation

1 | INTRODUCTION

Aggregation is a major challenge in the manufacturing of therapeutic proteins (Randolph & Carpenter, 2007; Roberts, 2014; Wang, 1999). Numerous stresses encountered during protein production cause aggregation. These different stresses (e.g., freeze-thawing; Arsiccio & Pisano, 2017; Barnard, Singh, Randolph, & Carpenter, 2011; Twomey, Less, Kurata, Takamatsu, & Aksan, 2013, interactions at air-water and container-water interfaces; Cordes, Carpenter, & Randolph, 2012; Ludwig, Carpenter, Hamel, & Randolph, 2010; Sethuraman, Morcone, & Belfort, 2004; Sluzky, Klibanov, & Langer, 1992; Webb, Cleland, Carpenter, & Randolph, 2002, exposure to excipient degradation products such as those from polysorbates; Ha, Wang, & Wang, 2002; Kerwin, 2008; Wasylaschuk et al., 2007, pH extremes; Chi, 2004; Thrumangalathu, Krishnan, Brems, Randolph, & Carpenter, 2006, and elevated temperatures) produce polydisperse distributions of aggregates (Joubert, Luo, Nashed-Samuel, Wypych, & Narhi, 2011). As a result, aggregates may be observed in protein formulations following purification (Arakawa, Ejima, & Akuta, 2017), filtration (Barnard, Kahn, Cetlin, Randolph, & Carpenter, 2014;
Liu, Randolph, & Carpenter, 2012; A. Sharma, Anderson, & Rathore, 2008), pumping (Saller et al., 2016; Tyagi et al., 2009; Tzannis, Hrusesky, Wood, & Przybycien, 1996), freezing (Barnard et al., 2011; Kolhe, Amend, & Singh, 2010; Kuelzto, Wang, Randolph, & Carpenter, 2008; Vlueland et al., 2018), vial filling (Nayak, Colandene, Bradford, & Perkins, 2011), viral clearance steps and shipping (Siska, Carpenter, & Randolph, 2010; Freitag et al., 2015; Jiskoot et al., 2016; Rosenberg, 2006) has generated interest in developing techniques to identify their root causes.

The root cause of protein aggregation is often elusive. However, the various stresses that promote protein aggregation each induce aggregation by somewhat different molecular mechanisms (Roberts, 2007; Wang & Roberts, 2018). These distinct mechanisms lead to particle populations whose size and morphology distributions comprise particle "fingerprints" that reflect the root cause of their formation. Better techniques for characterizing these particle fingerprints would provide methods to rapidly determine the root causes of particle formation in a sample.

Flow imaging microscopy (FIM) is a commonly used technique for analyzing size distributions of protein aggregates (Narhi et al., 2015; D. K. Sharma, King, Oma, & Merchant, 2010; D. K. Sharma, Oma, Pollo, & Sukumar, 2010; Zölls et al., 2013) and other particles. FIM uses light microscopy combined with microfluidics to capture digital images of particles larger than 1 µm in size contained within a sample. The output from this instrument is a set of digital images of individual particles in a small liquid sample (usually about $10^3$ to $10^5$ images per 200 µl sample). The images contain a large amount of morphological information. However, in common practice, most of the morphology information potentially available from FIM measurements is not utilized.

Convolutional neural networks (ConvNets) can be used to extract and analyze morphological information embedded in FIM images (Calderon, Daniels, & Randolph, 2018; Gambe-Gilbuena, Shibano, Krayukhina, Torisu, & Uchiyama, 2020). ConvNets are a family of neural networks capable of learning relevant features from a collection of images that are useful when performing tasks such as classification and dimension reduction (Calderon et al., 2018; Esteva et al., 2017; Krizhevsky, Sutskever, & Hinton, 2012; Schroff, Kalenichenko, & Philbin, 2015). ConvNets trained on FIM data sets can accurately classify protein aggregates produced by different stresses. In Calderon et al. (2018) and Gambe-Gilbuena et al. (2020), a set of single, well-defined stresses (e.g., freeze-thawing and heating) was applied to protein solutions, causing aggregates to form. ConvNets were then trained on FIM images of the resulting particles to train classifiers to recognize particle morphologies generated by one of these stresses. The resulting classifiers were then used to classify FIM images of particles from new samples that had been subjected the same set of stresses.

Although these previous approaches are useful for analyzing protein aggregates within formulations exposed to single stresses, protein aggregates encountered in practice are likely the result of a superposition of a variety of stresses, yielding more varied fingerprints. The potentially large number of different aggregate sources may mask subtle but relevant changes in particle populations due to minor changes in process conditions such as changes in container-closure systems. This issue is compounded by the inherent variability in particle morphology even under tightly controlled conditions (Gambe-Gilbuena et al., 2020). Thus, it can be difficult to determine if morphology differences within a particle population reflect different root causes of aggregation or merely sample-to-sample variability.

In the present study, we demonstrate a ConvNet algorithm that can be used to quantitatively determine if particle morphologies recorded in a small collection of FIM images are statistically different from those generated under a user-defined baseline condition. This analysis uses a combination of dimension reduction and hypothesis testing. Facial recognition strategies (Sun, Chen, Wang, & Tang, 2014; Taigman, Yang, Ranzato, & Wolf, 2014) such as triplet loss approaches (Schroff et al., 2015) can reduce the dimensionality of FIM image data sets, compressing the information contained in color FIM images to two-dimensional (2D) feature vectors (i.e., the fingerprints). The extreme information compression enables the use of nonparametric techniques such as kernel density estimates of the probability density of these low-dimensional representations for particles made under a single baseline condition. Goodness-of-fit hypothesis test with user-tunable false-positive rates can then be used to compare collections of particle images from other samples to this density.

One potential application of this approach is testing whether formulation design decisions (e.g., pH, excipient concentrations, container-closure types) affect protein aggregate populations. In this study, we focus on the impact of container-closure systems on protein aggregate morphology. The geometry and chemistry of the container can affect protein aggregation (Kiese, PappenBerger, Friess, & Mahler, 2008). Container-induced particles may come directly from the container (e.g., glass flakes from delamination in glass vials; Ennis et al., 2001) as well as from protein aggregates triggered by the container itself (Bee, Randolph, Carpenter, Bishop, & Dimitrova, 2011; Gerhardt et al., 2014). Aggregation may depend not only on the type of container (Krayukhina, Tsumoto, Uchiyama, & Fukui, 2015; Kumru et al., 2012; Teska, Brake, Tronto, & Carpenter, 2016) but also may vary between different lots of the same container from a given manufacturer.

## MATERIALS AND METHODS

### 2.1 Materials

Intravenous immunoglobulin (IVig, Gammagard Liquid) was obtained from Takeda International (Lexington, MA). Phosphate-buffered saline (PBS) containing 144 mg/L potassium phosphate monobasic, 795 mg/L potassium phosphate dibasic, and 9,000 mg/L sodium chloride at pH 7.4 was obtained from Gibco (Waltham, MA). Polypropylene, 2 ml microcentrifuge tubes ("Plastic") were from Fisher Scientific (Waltham, MA). FIOlAX Clear 3 ml type 1 borosilicate glass...
vials ("Glass 1") were obtained from Schott (Elmsford, NY). A second 3 ml type 1 borosilicate glass vial ("Glass 2") was obtained from Duran Wheaton Kimble (Mainz, Germany). Micro-90 was obtained from International Products Corp. (Burlington, NJ). Polystyrene 20-µm calibration beads were from Thermo Fisher Scientific (Waltham, MA).

### 2.2 | Generation of protein aggregates

IVIg aggregates were made using combinations of two aggregation-inducing stresses in three container types. Five experimental replicates were made per combination of container and stress. In each replicate, two containers were cleaned by filling the container with ultrapure water generated using a PURELAB flex 1 water deionization system from ELGA Labwater (Wycombe, UK), shaking the filled container, then emptying the container and allowing the container to air dry for 1 hr. IVIg stock solution was made by centrifuging the as-received drug product containing 100 mg/ml IVIg at 15,000 g for 20 min at 4°C. The supernatant was then diluted to 0.5 mg/ml using filtered PBS, and 1.5 ml of this solution was filled into each container. Samples were then exposed to either freeze-thawing or shaking stresses as described below.

### 2.3 | Freeze-thaw stress

Samples stressed by freeze-thawing underwent four freeze-thaw cycles. During each cycle, the samples were suspended in a fixed orientation in liquid nitrogen for 4 min and then suspended in a 30°C water bath for 10 min. FIM analysis was performed immediately after the final freeze-thaw cycle was completed.

### 2.4 | Shaking stress

Samples were taped in a horizontal orientation onto an orbital plate shaker and shaken at 800 rpm for 4 hr. FIM analysis was performed immediately after the shaking was completed.

### 2.5 | FIM

FIM images were recorded with a FlowCam® VS instrument (Fluid Imaging Technologies, Inc., Scarborough, ME) with a ×10 objective, a field-of-view flow cell with a depth of 80 µm and width of 700 µm, and color imaging. The instrument was focused using the built-in autofocus protocol for optimal image quality using 20-µm calibration beads. 1% Micro-90 solution followed by filtered ultrapure water were flushed through the instrument before and between measurements. The flash duration of the instrument was adjusted between replicates to achieve a constant background intensity of 150. Three 0.2 ml aliquots were analyzed from each replicate vial. Images were collected at a flow rate of 0.05 ml/min using 15 light and 17 dark pixel thresholds for particle segmentation.

### 2.6 | Image postprocessing

FIM images of particles were imported into Python 2.7. Before further analysis, the size of each image was adjusted to 24 × 24 pixels. Smaller images were padded with pixels sampled from a normal distribution with the same mean and variance as the border of the image and smoothed using Gaussian smoothing. For larger images a centered 24 × 24 crop of the image was used. Three experimental replicates for each combination of container and stress were used to train the algorithm, while the remaining two independent replicates were retained for use in subsequent testing. Fourteen thousand images were randomly selected from each of the three training replicates to be used as training data for the algorithm described in the next section. The remaining two replicates for each condition were not shown to the algorithm at all during training. Two thousand images from each replicate, including those not included in algorithm training, were set aside during algorithm training and used to test the performance of the trained algorithm.

### 2.7 | Algorithm overview

An algorithm was developed to determine if FIM images from a test sample were statistically consistent with those in a baseline sample. Hereafter, we refer to these FIM images as "particles" since each FIM image is recorded on a single particle. Figure 1 shows the process of training the algorithm to identify particles in a baseline sample. First, a ConvNet is trained on the collection of FIM images (Figure 1, first row, first column) to compress information within these images into a low-dimensional (2D here) point cloud of embeddings (Figure 1, second row, first column). A nonparametric kernel density estimate is then constructed from this low-dimensional point cloud to estimate the probability density of embeddings in the baseline sample (Figure 1, second row, second column). The estimated probability density is subsequently used to define a Rosenblatt transform which maps an embedding to a new random vector having the same dimensions of the embedding point (Rosenblatt, 1952; Figure 1, second row, third column). Goodness-of-fit hypothesis tests can be applied in conjunction with this Rosenblatt transform to determine if sets of FIM image embeddings points are consistent with the estimated baseline density. The hypothesis test exploits the following mathematical fact: if a collection of embedding points are distributed according to the probability density associated with the baseline sample, the Rosenblatt transform yields multivariate random vectors whose components are independent and identically distributed with each component being a uniformly distributed random variable between 0 and 1. Goodness-of-fit hypothesis testing can formally check sets.
of transformed embeddings for this property. Critical values for this hypothesis test are set by repeatedly subsampling Rosenblatt-transformed embedding points from the baseline sample, calculating test statistics for each subsample, selecting a value based on the resulting test statistic distribution to obtain a user-specified type I error (i.e., false-positive) rate (Figure 1, first row, third column).

Once trained, the algorithm can be used to quantify how statistically similar particle populations in test samples are to that in the baseline sample. Figure 2 shows the application of the trained algorithm to test samples containing either similar or different particle populations. To analyze a test sample, a small number of FIM images (e.g., 5–200) are subsampled from the test sample, converted to 2D embeddings with the trained ConvNet, and transformed using the Rosenblatt Transform defined by the baseline density. Goodness-of-fit hypothesis tests using the critical values from the baseline sample are then used to test if the transformed embeddings are consistent with a uniform distribution. Applying this algorithm to particles that resemble those in the baseline sample (Figure 2, top row) results in embeddings that are both visually and statistically consistent with those in the baseline sample. Conversely, particles that do not resemble the baseline sample (Figure 2, bottom row) yield embeddings less consistent with the baseline sample and are thus identified through goodness-of-fit hypothesis testing as a different particle population from the baseline sample.

2.8 | ConvNets

ConvNets are used in this analysis to extract and compress information in FIM images into a set of image features. While previously these image features were used as the input to a classifier that predicted the stress to which a sample had been exposed (Calderon et al., 2018), in the current analysis nonparametric techniques were used to estimate the distribution of these features. To apply these techniques, the ConvNet needed to be trained to learn extremely low-dimensional (i.e., 2–3 image features) representations of FIM images to avoid the exponential decrease in accuracy of these techniques with each additional dimension in the data (Scott, 2015).

The ConvNet used in this analysis was trained using a triplet loss algorithm, an approach that was developed for facial recognition to learn highly compressed image representations (Schroff et al., 2015). In this algorithm, a ConvNet is trained to learn a low-dimensional representation or embedding of images that acts to cluster together images from similar sources (e.g., faces of the same person, or protein aggregates made by the same stress and in the same container). During training, triplets (i.e., sets of three images) are assembled from the training data consisting of an image of one particle type (the anchor image), another image of the same particle type (a positive image), and a third image of a different particle type (the negative image). These triplets are fed through the neural network to calculate embeddings for each of the three images. The network’s parameters

**FIGURE 1** Flowchart showing how the algorithm is trained to detect particle populations similar to those made under some baseline condition. FIM images of particles made under the baseline condition (first figure) are used to train a ConvNet capable of compressing the image into a two-dimensional (2D) embedding (second figure). The probability density of these embeddings is then estimated using a kernel density estimate (third figure). A Rosenblatt transform defined using this distribution can then be used to map embeddings from the baseline sample onto a uniform distribution (fourth figure). The transformed embeddings can then be used to set up goodness-of-fit hypothesis tests by estimating the distribution of a test statistic for the baseline sample (fifth figure, curve) and using the distribution to determine an appropriate critical value for the test (fifth figure, dashed line). ConvNet, convolutional neural networks; FIM, flow imaging microscopy [Color figure can be viewed at wileyonlinelibrary.com]
are then adjusted to minimize a modified triplet loss function (Hermans, Beyer, & Leibe, 2017):

\[ l = \ln(\exp(-\alpha(d_{ap} - d_{an}) + 1)) \]

where \( l \) is the triplet loss, \( d_{ap} \) is the Euclidian distance between the representations of the anchor and positive images returned by the ConvNet, \( d_{an} \) the distance between the representations of the anchor and negative image, and \( \alpha \) is the margin, a small number used to scale the distances between dissimilar particle types in the embedding. This loss function is minimized when particles from a common source are close to each other in the embedding space and far apart from particles from other sources. In addition to allowing nonparametric density estimation techniques to be used, the resulting ConvNet can also be used to effectively analyze FIM image types not shown to the network during training. The algorithm identifies that the particles in the test sample are consistent with the baseline sample.

The ConvNet was trained on FIM images of particles produced in Plastic and Glass 1 vials after applying either freeze-thaw or shaking stresses. Particles generated within Glass 2 vials were not used to train the ConvNet, but instead were used to test the network’s generalization to unseen particle types. The network was trained with a margin of 0.5 using minibatches of 64 triplets using an Adam optimizer (Kingma & Ba, 2015) with a 0.001 learning rate. Triplet minibatches were generated by assembling minibatches of 64 anchor images from the training images and calculating image embeddings for each training image at the start of each epoch. Positive and negative images for each anchor image were then randomly selected from all training images until a triplet was found that met semihard triplet mining criteria (Schroff et al., 2015) based on the most recently calculated embeddings. This approach filters out triplets that have low and high values of the loss function which can prevent the network from learning effective image representations. The current value of the triplet loss function, as well as the variance in embeddings from each condition, was monitored during training at the end of each epoch. The network was trained for 100 epochs and the network parameters that minimized the triplet loss was used in subsequent steps of the analysis.

FIGURE 2 Flow chart showing the application of the algorithm to test samples that either resemble the baseline sample (top row) or do not resemble the baseline sample (bottom row). To perform the analysis small sets of images are selected from each sample (first column) and analyzed with the ConvNet to obtain two-dimensional embeddings for the images (second column, points). These embeddings are then compared against the distribution of embeddings for the baseline sample (second column, contour) using a combination of Rosenblatt transforms and hypothesis testing (third column). If the test statistic for the test sample (third column, solid line) is less than critical value for the baseline sample (third column, dashed line), the algorithm identifies that the particles in the test sample are consistent with the baseline sample. ConvNet, convolutional neural networks; FIM, flow imaging microscopy [Color figure can be viewed at wileyonlinelibrary.com]
Kernel density estimation is a nonparametric technique for estimating the probability density function (PDF) of a data set using data sampled from this distribution (Scott, 2015). This technique was used to estimate the distribution of the low-dimensional FIM image embeddings for the baseline sample directly from the embeddings. Embedding sets from test samples were then compared against this distribution to decide if the particles in the test sample were consistent with those in the baseline sample.

Kernel density estimates of the distribution of embeddings for the baseline sample were constructed using a product kernel and using normal distributions as the kernel in each dimension. This kernel function was chosen so that the estimated PDF has an infinite support, which was helpful in obtaining meaningful evaluations of the Rosenblatt transform on particles that embedded far away from the mode of the PDF. The bandwidth of the kernel in each dimension was calculated using a normal reference rule (Scott, 2015):

$$h_i = \left(\frac{4}{d + 2}\right)^{1/(d + 4)} \sigma_i n^{-1/(d + 4)},$$  \hspace{1cm} (2)

where $h_i$ is the bandwidth in dimension $i$, $d$ is the number of dimensions of the embeddings (2 in this study), $n$ is the number of datapoints used to construct the density estimate, and $\sigma_i$ is the standard deviation of the embeddings in dimension $i$.

2.11 | Goodness-of-fit hypothesis testing

After applying the Rosenblatt Transform defined by the density estimate for the baseline sample to image embeddings from the test sample, goodness-of-fit hypothesis tests were used to test the null hypothesis that the transformed embeddings are consistent with a uniform distribution. Rejection of this null hypothesis indicated that the particles in the test sample were not consistent with those in the baseline sample and thus potentially formed under a different set of conditions.

All goodness-of-fit hypothesis testing was performed using a Kolmogorov–Smirnov (KS) test (Darling, 1957), a one-dimensional test to assess the hypothesis that the transformed embeddings are consistent with a uniform distribution.

### Table 1: ConvNet structure used in this study

<table>
<thead>
<tr>
<th>Layer no.</th>
<th>Layer type</th>
<th>No. of features</th>
<th>Feature size</th>
<th>Activation</th>
<th>Input shape</th>
<th>Output shape</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Convolutional</td>
<td>32</td>
<td>$3 \times 3$</td>
<td>ReLU</td>
<td>$24 \times 24 \times 3$</td>
<td>$22 \times 22 \times 32$</td>
</tr>
<tr>
<td>2</td>
<td>Convolutional</td>
<td>32</td>
<td>$3 \times 3$</td>
<td>ReLU</td>
<td>$22 \times 22 \times 32$</td>
<td>$20 \times 20 \times 32$</td>
</tr>
<tr>
<td>3</td>
<td>Dropout (10% rate)</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>$20 \times 20 \times 32$</td>
<td>$20 \times 20 \times 32$</td>
</tr>
<tr>
<td>4</td>
<td>Convolutional</td>
<td>32</td>
<td>$3 \times 3$</td>
<td>ReLU</td>
<td>$20 \times 20 \times 32$</td>
<td>$18 \times 18 \times 32$</td>
</tr>
<tr>
<td>5</td>
<td>Convolutional</td>
<td>64</td>
<td>$3 \times 3$</td>
<td>ReLU</td>
<td>$18 \times 18 \times 32$</td>
<td>$16 \times 16 \times 64$</td>
</tr>
<tr>
<td>6</td>
<td>Max pooling (2 × 2)</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>$16 \times 16 \times 64$</td>
<td>$8 \times 8 \times 64$</td>
</tr>
<tr>
<td>7</td>
<td>Dropout (10% rate)</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>$8 \times 8 \times 64$</td>
<td>$8 \times 8 \times 64$</td>
</tr>
<tr>
<td>8</td>
<td>Convolutional</td>
<td>64</td>
<td>$3 \times 3$</td>
<td>ReLU</td>
<td>$8 \times 8 \times 64$</td>
<td>$6 \times 6 \times 64$</td>
</tr>
<tr>
<td>9</td>
<td>Convolutional</td>
<td>64</td>
<td>$3 \times 3$</td>
<td>ReLU</td>
<td>$6 \times 6 \times 64$</td>
<td>$4 \times 4 \times 64$</td>
</tr>
<tr>
<td>10</td>
<td>Flatten</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>$4 \times 4 \times 64$</td>
<td>$1,024$</td>
</tr>
<tr>
<td>11</td>
<td>Dropout (10% rate)</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>$1,024$</td>
<td>$1,024$</td>
</tr>
<tr>
<td>12</td>
<td>Dense</td>
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<td>n/a</td>
<td>Softplus</td>
<td>1,024</td>
<td>64</td>
</tr>
<tr>
<td>13</td>
<td>Dense</td>
<td>2</td>
<td>n/a</td>
<td>None</td>
<td>64</td>
<td>2</td>
</tr>
</tbody>
</table>

Abbreviations: ConvNet, convolutional neural network; ReLU, rectified linear unit.
(1D) goodness-of-fit hypothesis test that compares the cumulative distribution function (CDF) of the embeddings to the CDF of a 1D uniform distribution. Two 1D KS tests were performed on each dimension of the transformed embeddings to test the null hypothesis as the dimensions of the transformed embeddings are independent under the null hypothesis. The null hypothesis was rejected if either dimension was not consistent with a uniform distribution. The desired overall type I error (i.e., false-positive) rate of the test can be used to set error rates for the two individual tests obtained using the Bonferroni correction. The overall null hypothesis was rejected if either of the two tests rejected the null hypothesis. A 5% overall type I error rate was used in this analysis.

Test statistics for the hypothesis test were calculated using sets of a small number (e.g., 5–200) of particles randomly selected from the test sample. Since the statistical power of these hypothesis tests scales with the number of data points used in the analysis, restricting the number of particles that are analyzed at once helped control the sensitivity of the analysis. In this study sets of either 20 or 200 particles were used to compare test samples to the baseline sample.

Monte Carlo simulations were used to select appropriate critical values (aiming at obtaining a user-specified type I error rate) of the test statistic to account for the bias introduced by both the non-parametric density estimate and subsampling scheme. The test statistic distribution for sets of 20 particles was estimated by randomly subsampling 10,000 sets of 20 training particles from the baseline condition and evaluating the test statistics for each subsample. These distributions were then used to select critical values at the appropriate significance level for each test. This process was repeated using sets of 200 particles, resulting in a second test statistic distribution and critical value for these larger particle sets.

Test samples were compared against baseline samples by repeatedly subsampling sets of particles from the test sample and using the algorithm to identify the fraction of these subsamples that were consistent with the baseline sample. 2,500 sets of either 20 or 200 particles were subsampled from the test sample. After computing the Rosenblatt transformed embeddings for each subsample, the hypothesis test was used to determine if each subsample was consistent with the baseline sample. The similarity between the test sample and the baseline sample using a given number of particles was recorded as whether or not the subsample was consistent with the baseline sample. The similarity between the test sample and the baseline sample was estimated by randomly subsampling sets of particles from the test sample and using the algorithm to identify sets of either 20 or 200 particles that resemble sets of the particles made in each of the three containers after exposure to each stress to samples of those made in each of the three containers after exposure to the same stress.

2.12 Particle morphology comparison

The algorithm described above was used to compare samples of aggregated IVlg formed under different stress conditions and in different containers. A ConvNet was trained on FIM images of particles made in Plastic and Glass 1 containers with a triplet loss approach. The remaining steps of the algorithm were then trained to identify sets of either 20 or 200 particles that resemble sets of the corresponding number of particles made in one container after exposure to one stress. These later steps were separately trained 12 times to cover the six possible baseline classes (particles made by one stress in one container) and the two-particle set sizes (20 or 200) that were used during testing.

The trained algorithms were used to investigate the impact of different stresses and different containers on particle morphology. This comparison was performed by comparing small sets of test particles from each sample to all the training particles from a single container and stress. To investigate the impact of stresses on particle populations, the algorithm was used to compare particles generated by freeze-thaw stress (the baseline stress class) in each of the three containers to particles made in the same container type after exposure to shaking and freeze-thaw stresses. Similarly, the effect of container on particle populations was investigated by comparing particles made in Glass 1 containers after exposure to each stress to samples of those made in each of the three containers after exposure to the same stress.

2.13 Surface characterization

The two glass vial types used in this analysis were characterized using contact angles and surface profilometry. Each of these measurements was performed by cutting off the bottom of the vial and cleaning the inner surface with ethanol, water, and nitrogen before measurements.

To assess the hydrophobicity of the glass containers, contact angles were measured for each vial using a ramé-hart Model 210 goniometer/tensometer with DROPimage Pro software (Succasunna, NJ). This instrument was used to measure static, advancing, and receding contact angles on each of the three surfaces. These measurements were performed in triplicate. Between measurements, the surfaces were cleaned with ethanol, water, and nitrogen gas.

Surface profilometry was performed with a Dektak 3030 Profilometer (Billerica, MA) to measure the roughness of the two vials. Surface profiles were measured along a flat 1 mm length along the inner surface of the vial. These profiles were fitted to a second-degree polynomial which was then subtracted from the raw data to account for the macroscopic curvature of these surfaces. The flattened surface profiles were then used to calculate the arithmetic average roughness $R_a$ of each container which is calculated using:

$$R_a = \frac{1}{n} \sum_{i=1}^{n} |h_i|,$$  \hspace{2cm} (3)

where $n$ is the total number of locations along the 1 mm length that the height was measured, $i$ indexes the different height measurements, and $h_i$ is the height measured at point $i$.

3 RESULTS

3.1 FIM

Figure 3 shows collections of randomly selected FIM images obtained from each of the six conditions compared in this analysis.
These images reveal obvious differences between particles generated by freeze-thawing and shaking stresses; particles observed after shaking (Figure 3a-c) are typically large and exhibit complex morphologies while particles imaged after freeze-thaw cycling (Figure 3d-f) are much smaller with simple morphologies. Conversely, the effect of different containers on particle morphologies generated by these stresses is not visually obvious from the images.

3.2 | ConvNets

Figure 4 shows contour plots of the distribution of embeddings returned by the trained ConvNet for particles made by freeze-thawing and shaking stresses. The contours for the different stresses are visually separated within this embedding space, indicating that the network can distinguish between particles generated by shaking and freeze-thaw stresses. Figure 4 also shows sample particles that are mapped to different locations in the embedding space. In this embedding scheme, small particles with simple but common structures are mapped near the mode of the freeze-thaw distribution whereas large, complex heterogeneous particles are mapped near the mode of the shaking distribution.

Figure 5 shows contour plots of the estimated PDF of embeddings returned by the trained ConvNet for all particles not included in the network—including those from the four samples per condition that were not used to train the network. Figure 5a shows the embeddings for particles formed in Plastic containers, Figure 5b shows those formed in Glass 1 containers, and Figure 5c shows those formed in Glass 2 containers. These contour plots indicate an observable difference in the particle morphologies produced in the three containers as a result of shaking stresses. Compared with particles produced by shaking Glass 2 or Plastic containers, particles produced by shaking samples in Glass 1 containers (Figure 5b) have a much tighter density in the embedding space than either of the other samples. Particles produced by freeze-thawing stress appear to be influenced to a lesser extent by the container in which they were formed; particles produced freeze-thaw cycling in Glass 1 containers exhibit a slightly more diffuse distribution than those produced in the other container types (Figure 5b).
3.3 Particle comparisons

The remaining steps of the algorithm were used to compare the particle populations produced within different containers when exposed to different stresses. This comparison was done by choosing one of the samples being compared to be the baseline sample, subsampling small sets of particles from the other (test) sample, and testing the null hypothesis that each subsample contained particles that were consistent with those in the baseline sample. Table 2 shows the rejection frequencies when comparing sets of 20 particles from each of the three containers to those made by applying freeze-thaw stress to the same container. As was expected from both the raw flow imaging data shown in Figure 3 and the embeddings in Figure 5, the algorithm can easily identify morphology differences between particle populations that had been exposed to these two stresses using only a small number of particle images. Additionally, the algorithm only misidentified unseen test particles made under baseline conditions as being different from the baseline population around 5% of the time—the type I error rate that the test was designed to give.

Table 3 shows the rejection frequencies when comparing sets of either 20 or 200 test particles made by each stress to those produced in Glass 1 containers when exposed to the same stress. Interestingly, the ability of the algorithm to distinguish between particles produced in each of the three containers depended on the applied stress. Sets of 20 particles produced by exposing IVIG solutions in Plastic or Glass 2 containers to freeze-thawing stress were only able to be distinguished from those produced in Glass 1 containers at approximately the same rate as the type I error rate. In contrast, sets of 20 particles produced by shaking stress in each container were distinguishable from those made in Glass 1 containers approximately 40% of the time—eight times the type I error rate of the test. Increasing the size of the particle sets to 200 increased the fraction of shaking particle sets from Glass 2 and Plastic containers that were distinguishable from those produced in Glass 1 containers with only a small increase in the false positive rate when the test was applied to held-out baseline samples. In addition, the larger particle sets allowed the algorithm to distinguish between particles made by freeze-thawing stress in Glass 1 and Glass 2 ~40% of the time and those produced in Glass 1 and Plastic 20% of the time.
3.4 Surface characterization

Table 4 shows the surface characterization results for the two types of glass vials. The contact angle measurements suggest that the two glasses have similar hydrophobicities, with Glass 1 being slightly more hydrophilic than Glass 2. Both surfaces were also found to have similar roughnesses.

### Table 2

<table>
<thead>
<tr>
<th>Baseline sample:</th>
<th>Probability of rejecting test particle sets (20 particles)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Particles made by freeze-thaw stress in denoted container</td>
<td>Aggregates made by freeze-thaw stress</td>
</tr>
<tr>
<td>Glass 1</td>
<td>5.0%</td>
</tr>
<tr>
<td>Glass 2</td>
<td>5.9%</td>
</tr>
<tr>
<td>Plastic</td>
<td>5.0%</td>
</tr>
</tbody>
</table>

This study presents and demonstrates a novel algorithm designed to compare FIM images of protein aggregates and other particles obtained from one sample to those obtained in some baseline sample. This approach is a departure from previous techniques used to predict to which of a small set of conditions a sample was exposed (Calderon et al., 2018; Gambe-Gilbuena et al., 2020). The primary advantage of this new approach is its ability to determine, using only a small number of FIM images, if a new sample exhibits significantly different particle populations than those found under baseline conditions. The combination of traditional statistical tools with powerful machine learning algorithms can be used to determine if the two samples exhibit a morphology difference that cannot be explained by sample-to-sample variance in particle morphology under a single root cause. This approach is effective at identifying (statistically) significant differences in particle morphology occurring due to different root causes such as manufacturing changes or process upsets that could warrant further investigation.

The use of statistical tools in this algorithm also gives users control over the sensitivity of the analysis to changes in particle morphology. Decreasing the type I error rate or increasing the number of particles used in the hypothesis test increases the sensitivity of the test so that smaller deviations in particle morphology from the baseline condition are identified as significant. This feature allows the sensitivity of the algorithm to be tuned for a specific...
TABLE 3  Probability that a set 20 or 200 random particles formed in Glass 1, Glass 2, or Plastic containers by freeze-thaw or shaking stress will be distinguishable from a baseline population of particles made in the Glass 1 containers by the respective stress

<table>
<thead>
<tr>
<th>Container</th>
<th>Number of particles</th>
<th>Probability of rejecting test particle sets</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frozen-thaw</td>
<td>20</td>
<td>5.0</td>
</tr>
<tr>
<td></td>
<td>200</td>
<td>6.6</td>
</tr>
<tr>
<td>Shaking</td>
<td>20</td>
<td>5.1</td>
</tr>
<tr>
<td></td>
<td>200</td>
<td>4.0</td>
</tr>
</tbody>
</table>

TABLE 4  Contact angle and surface roughness measurements for Glass 1 and Glass 2 containers

<table>
<thead>
<tr>
<th>Container</th>
<th>Static contact angle</th>
<th>Advancing contact angle</th>
<th>Receding contact angle</th>
<th>Contact angle hysteresis</th>
<th>Ra (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Glass 1</td>
<td>16</td>
<td>23</td>
<td>&lt;5</td>
<td>&lt;18</td>
<td>28</td>
</tr>
<tr>
<td>Glass 2</td>
<td>27</td>
<td>31</td>
<td>&lt;5</td>
<td>&lt;26</td>
<td>12</td>
</tr>
</tbody>
</table>

application. For instance, the sensitivity of the algorithm can be increased for formulation development to better detect subtle changes in particle morphology between possible formulations. In contrast, in process monitoring applications the sensitivity of the algorithm can be decreased to minimize the chances that a false positive difference between a baseline “normal” reference batch and a new batch of product triggers unnecessary process shutdowns.

The techniques used to learn low-dimensional FIM image representations, calculate density estimates, and perform goodness-of-fit hypothesis testing were chosen to demonstrate the algorithm using relatively simple techniques. While the techniques used here were effective in this analysis, in practice other techniques for these analyses could be considered to further improve the performance of the algorithm. For example, different goodness-of-fit hypothesis tests (Anderson & Darling, 1954; Hong & Li, 2003; Justel, Peña, & Zamar, 1997) may provide better statistical power against deviations in particle morphology than the test used here.

The performance of this algorithm was demonstrated on particles made by subjecting IVIg solutions in three types of containers to two different stresses. Freeze-thawing and shaking stresses produced particle populations that would be easy to distinguish by visual inspection of the FIM images (Figure 3). These stresses produced visually resolved embeddings in the learned embedding space (Figures 4 and 5) which can then be easily distinguished using hypothesis testing (Table 2). It should be noted that this approach can still be used to classify samples by the stresses that they were exposed to as was done in previous papers (Calderon et al., 2018; Gambe-Gilbuena et al., 2020). If FIM images of different suspected stresses are available, this algorithm can be used to check if the particles in a sample are consistent with those produced by one of these stresses.

The algorithm was also able to identify the impact of container surfaces on particle populations. The results are shown in Table 3 suggest that the particle populations produced by freeze-thaw and shaking stress are influenced by the container, but that the effect is more obvious when shaking stress is used to create particles. The larger impact of the container on the particles produced by shaking stress agrees with the mechanistic understanding of these stresses. Agitation-induced aggregation likely occurs at interfaces including the air-water and container-water interfaces (Gerhardt et al., 2014; Teska et al., 2016). In contrast, during freeze-thawing aggregation due to adsorption to ice-water interfaces and cryoconcentration effects (Bhatnagar, Bogner, & Pikal, 2007) may occur at locations removed from container interfaces. Thus, the container interfaces might be expected to impact particle populations more when shaking stresses rather than freeze-thawing stresses are used to cause aggregation.

While the effect of container type was more subtle for particles made via freeze-thaw stress, the distribution of FIM image embeddings showed increased density near the mode of the distribution for Glass 2 vials as compared to that for Glass 1 vials (Figure 5). This difference was statistically discernible when sets of 200 particle images were analyzed. This result is somewhat surprising given the expected limited role of the container-water interface on aggregation induced by freeze-thawing. One possible explanation for the different particle fingerprints observed following freeze-thaw cycling in the two types of glass vials is differences in heat transfer through the vial walls. Differences in the thickness or geometry of the glass between the two vial types could cause a difference in the heat transfer rate through the container walls. Higher heat transfer rates would accelerate the growth of ice crystals from the walls of the container that occurs during liquid nitrogen-induced freezing (Searles, Carpenter, & Randolph, 2001). This faster growth results in a larger amount of ice interfacial area (Sarciaux, Mansour, Hageman, & Nal, 1999) and increased protein inclusion within growing ice crystals (Dong, Hubel, Bischof, & Aksan, 2009; Twomey et al., 2013) which can induce protein unfolding and aggregation (Strambini & Gabellieri, 1996; Strambini & Gonnelli, 2007).

The algorithm was not explicitly trained to detect the observed differences between particle populations produced in Glass 1 and 2 containers as particles generated in Glass 2 were not used to train the ConvNet embedding step. The ability to compare unseen particle types against those in a user-defined baseline allows new samples to be analyzed using a fraction of the FIM images (20–200) that would be required to retrain a ConvNet on a new particle type (>10,000).
The required number of FIM images can be recorded rapidly using small volumes of sample.

The algorithm revealed that different types of particles can form in a single protein formulation when stressed in different types of containers, even when the containers are as similar as the two borosilicate glass container types tested here. The container-dependent formation of different particles would have been difficult to predict using simple surface characterization techniques, since the glasses have similar roughness and hydrophobicity (Table 4).

The analysis presented here can be used to compare the effect of changes in container types (e.g., new lots of glass vials) on protein stability using an approach that incorporates standard accelerated stability protocols. Before any change, a baseline set of FIM images should be obtained after subjecting the protein formulation to accelerated stability conditions (e.g., agitation and freeze-thawing), capturing images of the resulting particles using FIM and training the algorithm to recognize the imaged particles. The accelerated stability protocol can then be repeated on a small number of containers in the new lot, and then the trained algorithm can be used to analyze whether new types of particles are associated with the new container lot. If the new container lot is found to produce statistically different particle populations, the lot may require additional characterization before use with the drug product.

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